

The Profit Equation

K_e	Cost of Equity	E	Equity
K_d	Cost of Debt	D	Long term Debt
K_a	Cost of Asset	V	Value of Asset ($V = D + E$)
ROA	Return on Asset	P	Profit
$\frac{D}{E} \cdot (ROA - i)$	Leverage factor	K_e^L	Cost of Equity of levered firm
$\frac{D}{E} \cdot (K_a - K_d)$	Leverage factor	K_e^U	Cost of Equity of unlevered firm - or - Cost of Asset - or - ROA
$\frac{D}{E} \cdot (K_e^U - K_d)$	Leverage factor		

Development

$$P = (ROA.V) - (K_d.D)$$

$$P = (K_a.V) - (K_d.D)$$

$$P = [K_a.(D + E)] - [K_d.D]$$

$$P = [K_a.D + K_a.E] - [K_d.D]$$

$$\frac{P}{E} = \frac{K_a.D}{E} + \frac{K_a.E}{E} - \frac{K_d.D}{E}$$

$$\frac{P}{E} = K_e = K_a \left[\frac{D}{E} + \frac{E}{E} \right] - K_d \cdot \frac{D}{E}$$

$$K_e = K_a \cdot \left[\frac{D}{E} + 1 \right] - K_d \cdot \frac{D}{E}$$

$$K_e = K_a \cdot \frac{D}{E} + K_a - K_d \cdot \frac{D}{E}$$

$$K_e = K_a + K_a \cdot \frac{D}{E} - K_d \cdot \frac{D}{E}$$

$$K_e = K_a + \frac{D}{E} (K_a - K_d)$$

-or-

$$ROE = ROA + \frac{D}{E} \cdot (ROA - i)$$

-or-

$$K_e^L = K_e^U + \frac{D}{E} \cdot (K_e^U - K_d)$$